SEARCH METHODS IN AI

GAME TREE SEARCH



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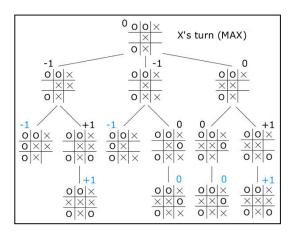
HEURISTIC SEARCH

- STATE or CONFIGURATION: \$ > A set of variables which define a state or configuration > Domains for every variable and constraints among variables to define a valid configuration STATE TRANSFORMATION RULES or MOVES: ~ ➤ A set of RULES which define which are the valid set of NEXT STATE of a given State It also indicates who can make these Moves (OR Nodes, AND nodes, etc) STATE SPACE or IMPLICIT GRAPH > The Complete Graph produced out of the State Transformation Rules. > Typically too large to store. Could be Infinite. INITIAL or START STATE(s), GOAL STATE(s) \sim SOLUTION(s), COSTS Depending on the problem formulation, it can be a PATH from Start to Goal or a Sub-graph of And-ed Nodes
 - ☐ (HEURISTICS)
 - Estimates of cost from a given state to goal. This, along with the current cost of the path from start till now is used to guide the search
- ☐ HEURISTIC SEARCH ALGORITHMS
 - Algorithm A*, Depth-First Branch & Bound, IDA*, AO*, Alpha-Beta, etc.
 - Knowledge vs Search



GAMES







Chess

2. player game
perfect information
win loss draw

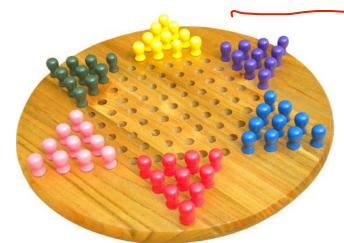
Tic-Tac-Toe

Go V

State

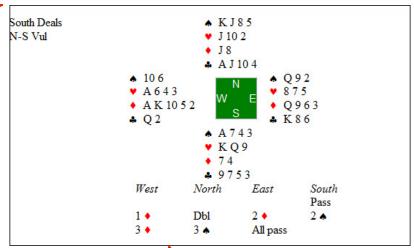
State Transformation Rules

MULTI-PLAYER GAMES



Chimese Checkers

Explayers perfect insprintant game



Bridge (Card Game)

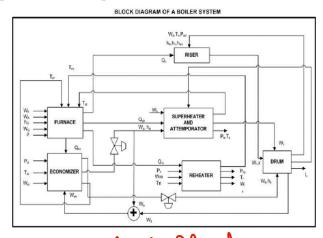
4 player

Two Teams incomplete information

PROBABILISTIC GAMES



outcome its based on chance. Driving 4 playors



Control Plant game with f contre an envoiment variables

ROBOT GAMES



Multiple players Simultaneously determints/probabilistic leams La collaboration

La competition

Spatio - temporal space

PRISONER'S DILEMMA

- Two members of a criminal gang are arrested and imprisoned. Each prisoner is in solitary confinement with no means of communicating with the other.
- The prosecutors lack sufficient evidence to convict the pair on the principal charge, but they have enough to convict both on a lesser charge.
- Simultaneously, the prosecutors offer each prisoner a bargain.

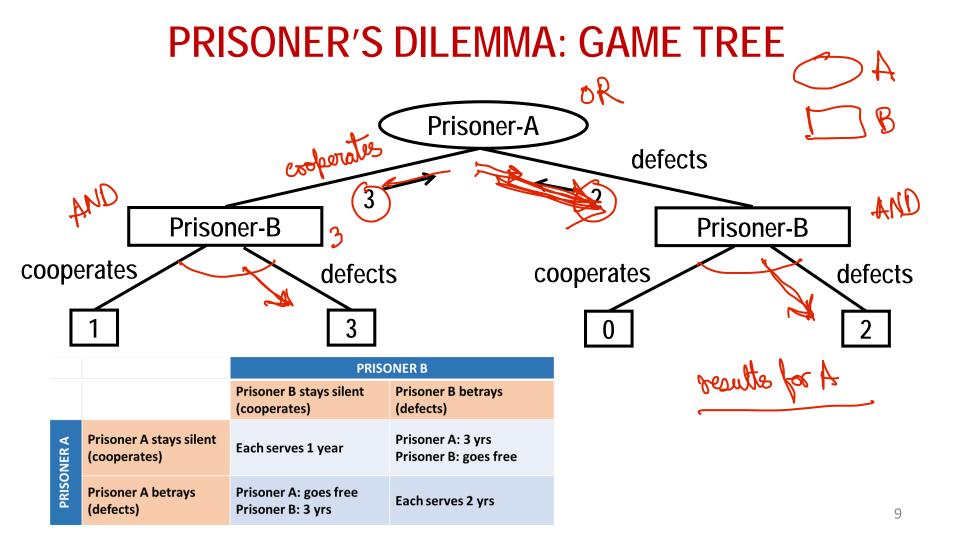
		PRISONER B				
		Prisoner B stays silent (cooperates)	Prisoner B betrays (defects)			
NERA	Prisoner A stays silent (cooperates)	Each serves 1 year	Prisoner A: 3 yrs Prisoner B: goes free			
PRISONER	Prisoner A betrays 🖔 (defects)	Prisoner A: goes free Prisoner B: 3 yrs	Each serves 2 yrs			

PRISONER'S DILEMMA: SOLUTION ARGUMENT

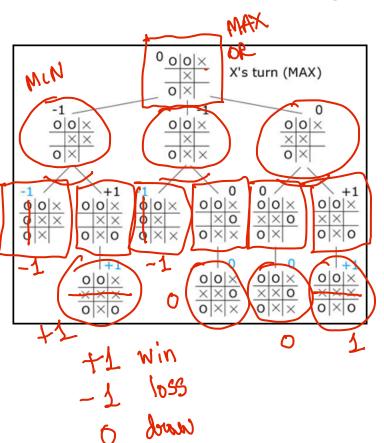
- Prisoner A will defect. Why?
 - Prisoner-A knows that Prisoner-B may cooperate or defect
 - If Prisoner-B cooperates, then by defecting, Prisoner-A will go free
 - If Prisoner-B defects, then Prisoner-A will face a longer sentence by staying silent
 - In both cases Prisoner-A gains by defecting

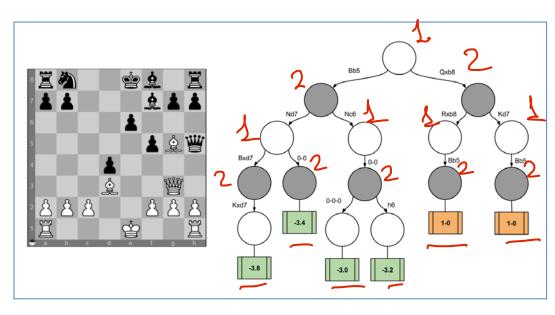
Therefore both prisoners will defect, although they would have gained from

C	oope	erating					ř
			PRISONER B				
			Prisoner B stays silent (cooperates)	t	Prisoner B betrays (defects)		
	NER A	Prisoner A stays silent (cooperates)	Each serves 1 year	7	Prisoner A: 3 yrs Prisoner B: goes free	•	3 45 1
	PRISONER	Prisoner A betrays (defects)	Prisoner A goes free Prisoner B: 3 yrs		Each serves 2 yrs	(2/13



TIC-TAC-TOE, CHESS

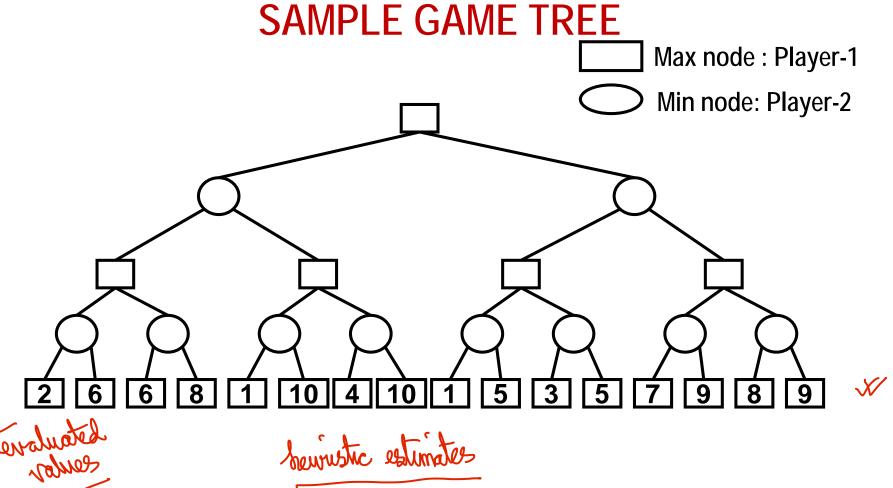




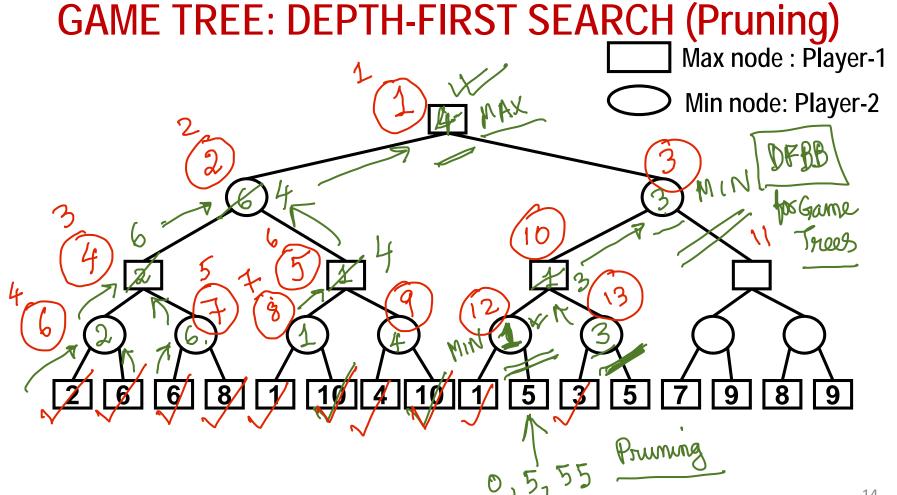
GAME TREES

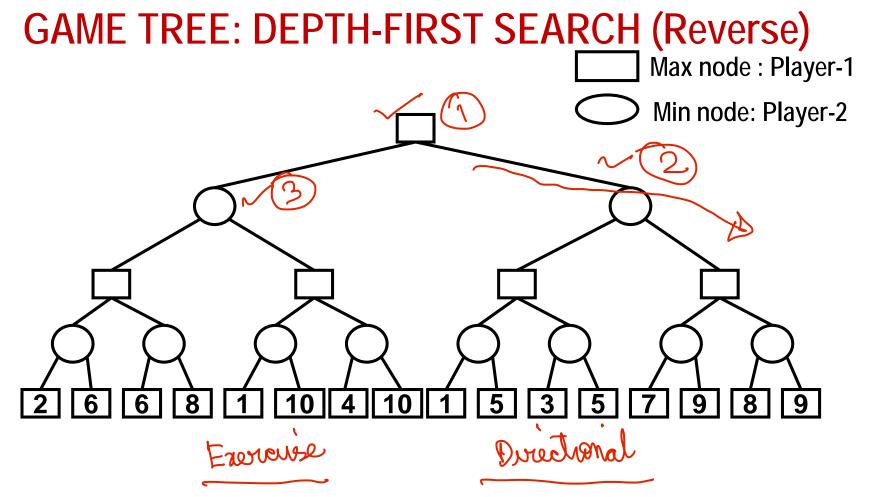
Player 2 Playor 21

- A tree with three types of nodes, namely (Terminal nodes) (Min nodes) and Max nodes. Terminal nodes have no children. The tree has alternating levels of Max and Min nodes, representing the turns of Player-1 and Player-2 in making moves
- All nodes represent some state of the game **
- Terminal nodes are labeled with the payoff for Player-1. It could be Boolean (such as WON or LOST). In large games, where looking ahead up to the WON / LOST states is not feasible, the payoff at a terminal node may represent a heuristic cost representing the quality of the state of the game from Player-1's perspective
- The payoff at a Min node is the minimum among the payoffs of its successors
- The payoff at a Max node is the maximum among the payoffs of its successors
- If Player-1 aims to maximize its payoff, then it represents Max nodes, else it represents Min nodes.

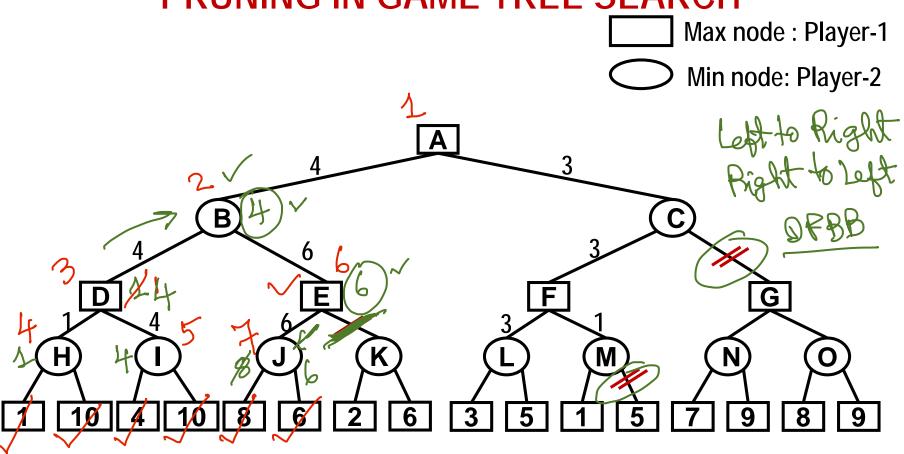


GAME TREE: MINMAX VALUE Max node: Player-1 Min-Max Value Min node: Player-2 MA AND OR OR

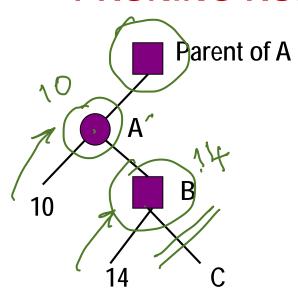




PRUNING IN GAME TREE SEARCH

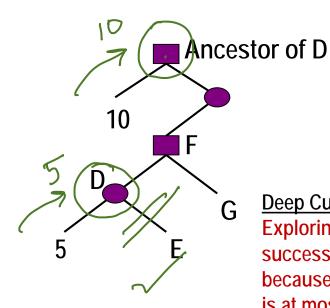


PRUNING RULES IN GAME TREE SEARCH



Shallow Cut-off

Exploring node C and its successors is meaningless because payoff at B is at least 14, and hence A will never choose the move to B.



Applicable in a similar manner for a Max node with Min Parent or **Ancestor**



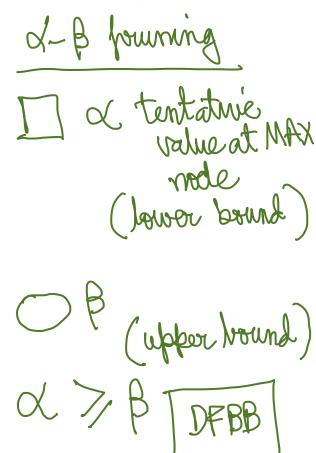


Deep Cut-off

Exploring node E and its successors is meaningless because the payoff at node D is at most 5, whereas the ROOT can already quarantee a payoff of 10 by choosing the left move. Therefore, the game will never reach the node D.

ALPHA-BETA PRUNING IN GAME TREE SEARCH

- Alpha Bound of $J(\alpha)$:
 - The max current payoff of all MAX ancestors of J (Lower Bound)
 - Exploration of a min node, J, is stopped when its payoff β (Upper Bound) equals or falls below alpha.
- Beta Bound of J (β):
 - The min current payoff of all MIN ancestors of J (Upper Bound)
 - Exploration of a max node, J, is stopped when its payoff α (Lower Bound) equals or exceeds beta
- In a max node, we update alpha or Lower Bound
- In a min node, we update beta or Upper Bound
- In both min and max nodes, we return when $\alpha \ge \beta$



ALPHA-BETA PRUNING PROCEDURE $V(J;\alpha,\beta)$

- 1. If J is a terminal, return V(J) = h(J).
- 2. If J is a max node: ~

For each successor J_k of J in succession:

Set
$$\alpha = \max\{\alpha\} V(J_k; \alpha, \beta)\}$$

If $\alpha \geq \beta$ then return β , else continue

Return α

3. If J is a min node:

For each successor J_k of J in succession:

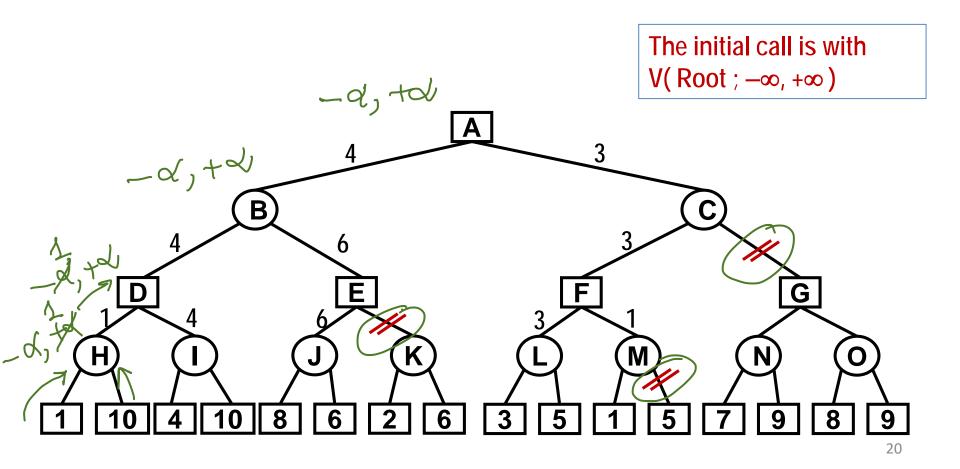
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Set \beta \neq \min \{ \beta, V(J_k; \alpha, \beta) \}
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If $\alpha \geq \beta$ then return α , else continue

Return B

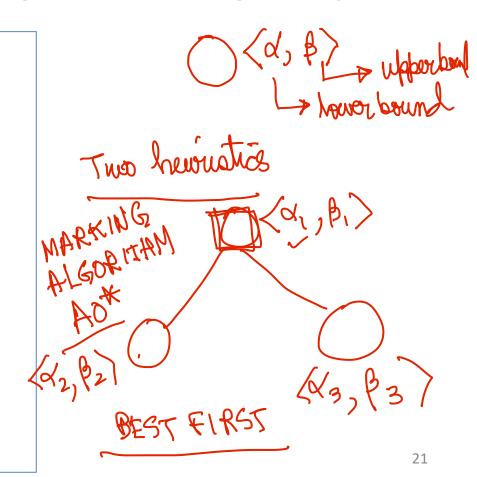
The initial call is with $V(Root; -\infty, +\infty)$

ALPHA-BETA PRUNING PROCEDURE $V(J;\alpha,\beta)$



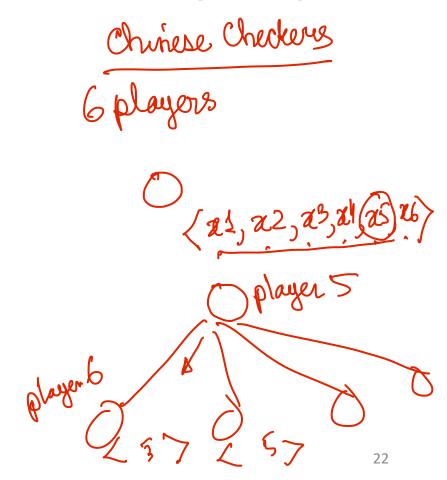
OTHER ASPECTS IN GAME TREE SEARCH

- Incorporate Heuristics in Game Trees
- Perform Best First Search in Game Trees
- Multi-Player Games for more than two players
- Team Games Cooperation and Competition
- Probabilistic Games
- Real Life Situations
 - Economics
 - Reactive Control Systems
 - Autonomous Systems



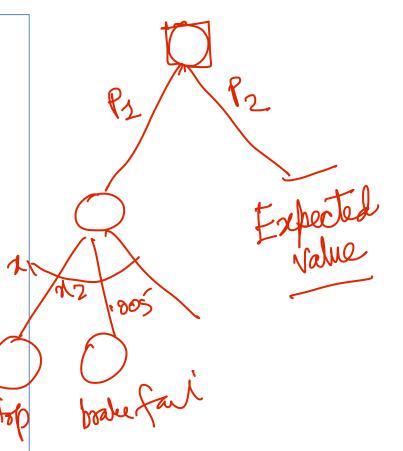
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Thank you